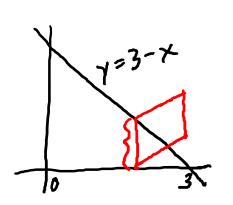
## Volume

$$V = \int_{a}^{b} A(x)dx$$

Find the area of a random cross section, then integrate it.

Ex. Find the volume of the solid with base the region bounded by y = 3 - x, x = 0, and y = 0 whose cross-sections are squares perpendicular to the *x*-axis.



3-×

 $V=\int \left( 3-x\right) ^{2}dx$ 

 $A=\left(3-\times\right)^{2}$ 

<u>Ex.</u> Base is the region bounded by  $y = 1 - x^2$  and the *x*-axis; cross-sections are isosceles right triangles with leg perpendicular to the *x*-axis.

 $\sqrt{2} = \int_{-\frac{1}{2}}^{\frac{1}{2}} (1-\chi^2)^2 d\chi$ 

 $A = \frac{1}{2} \left( \left| -x^{2} \right|^{2} \right)^{2}$ 

Ex. Base is the region bounded by x + y = 2 and the coordinate axes; cross-sections are semicircles with diameters perpendicular to the *y*-axis.

 $\sqrt{=\int_{\frac{1}{2}}^{\frac{1}{2}} \pi \left(\frac{2-\gamma}{2}\right)^2 dy$ x+γ=2 > x=2-γ  $A = \frac{1}{2} \pi \left(\frac{2-\gamma}{2}\right)^2$ 



Ex. Base is the region bounded by x + y = 2 and the coordinate axes; cross-sections are rectangles with heights that are 3 times the lengths that are perpendicular to the *y*-axis.

Xt.

 $V = \int 3(2-\gamma)^2 dy$ 

3(2-7)

 $A=3(2-y)^{2}$