Warm up Problems

1.
$$\int x^2 (2x^3 - 5)^5 dx$$

$$2. \int e^{-5x} dx$$

$$3. \int \frac{\sqrt{\ln x}}{x} dx$$

More Substitution

$$\frac{\text{Ex.} \int \tan x \, dx}{\int \cot x \, dx} = \int \frac{1}{\cot x} \sin x \, dx$$

$$u = \cos x$$

$$du = -\sin x \, dx$$

$$= -\ln |\cos x| + C$$

$$-du = \sin x \, dx$$

$$= \ln |\cos x|^{-1} + C$$

$$\int \tan x \, dx = \ln |\sec x| + C$$

$$\underline{\text{Ex.}} \int \frac{x}{x+3} \, dx$$

$$du = dx$$

$$du = dx$$

$$x = u - 3$$

$$\frac{\text{Ex.}}{\int \frac{x}{x+3} dx} = \int \frac{u-3}{u} du = \int \frac{u}{u} - \frac{3}{u} du$$

$$= \int (1-\frac{3}{u}) du$$

$$du = dx$$

$$= x - 3 \ln |y| + C$$

$$= x + 3 - 3 \ln |x + 3| + C$$

$$= x - 3 \ln |x + 3| + D$$

In a definite integral, you should find the antiderivative using substitution, change back to x, and then plug in endpoints.

$$\frac{Ex.}{\int xe^{x^2} dx}$$

$$= \int e^{x} \frac{1}{2} dx$$

$$= \frac{1}{2} e^{x^2} \frac{1}{2} e^{x^2}$$

$$= \frac{1}{2} e^{x^2} \left| \frac{1}{2} e^{x^2} \right|^2$$

$$= \frac{1}{2} e^{x^2} \left| \frac{1}{2} e^{x^2} \right|^2$$

$$= \int_{0}^{2} e^{4} \cdot \frac{1}{2} dn$$

$$= \frac{1}{2} e^{4} - \frac{1}{2} e^{0}$$

$$= \frac{1}{2} e^{2} - \frac{1}{2} e^{0}$$

$$= \frac{1}{2} e^{2} - \frac{1}{2} e^{0}$$

$$\frac{Ex.}{\int_{0}^{\pi/4} \tan^{3}\theta \sec^{2}\theta d\theta} = \frac{\pi}{4} \xrightarrow{u=1}^{\pi/4} \frac{du}{du}$$

$$= \int_{0}^{\pi/4} u^{3} du$$

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$$= \int_{0}^{\pi/4} u^{4/4} du$$

$$= \int_{0}^{$$

$$\frac{\Pr \cot x}{\int \frac{1}{5-x} dx} = \int_{1}^{3} \frac{1}{\sqrt{(-1)}} dx$$

$$\frac{1}{\sqrt{1-1}} = \int_{1}^{3} \frac{1}{\sqrt{1-1}} d$$

We could have changed the endpoints to u...