

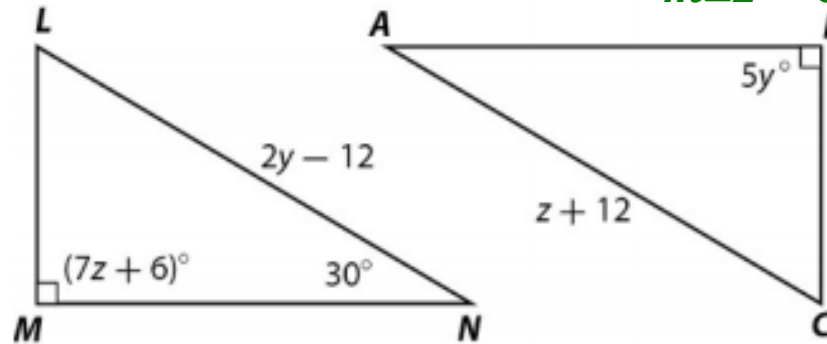
Warm Up

$\triangle LMN \cong \triangle CBA$. Find each value.

$$7z + 6 = 90$$

$$7z = 84$$

$$z = 12$$



$$90 + 30 + m\angle L = 180$$

$$120 + m\angle L = 180$$

$$m\angle L = 60$$

$$5y = 90$$

$$y = 18$$

1. $z = \underline{12}$

2. $y = \underline{18}$

3. $m\angle L = \underline{60^\circ}$

4. $LN = \underline{24}$

5. $m\angle C = \underline{60^\circ}$

6. $AC = \underline{24}$

$$LN = 2(18) - 12$$

$$LN = 24$$

$$m\angle C = m\angle L$$

$$m\angle C = 60$$

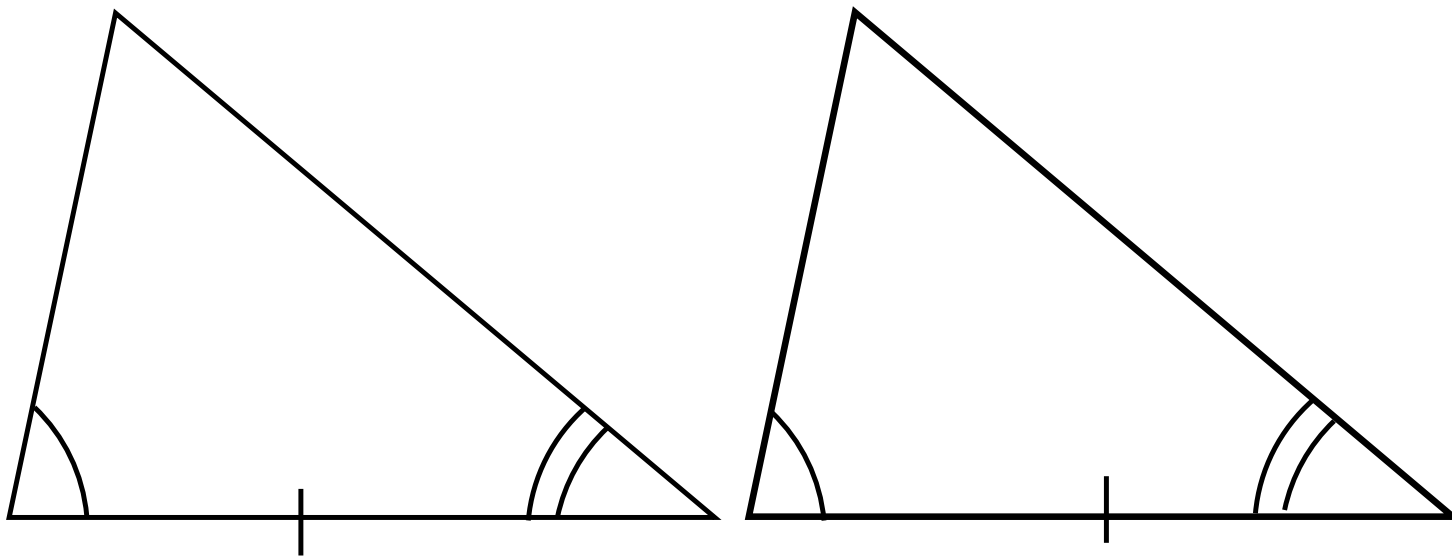
$$AC = 12 + 12$$

$$AC = 24$$

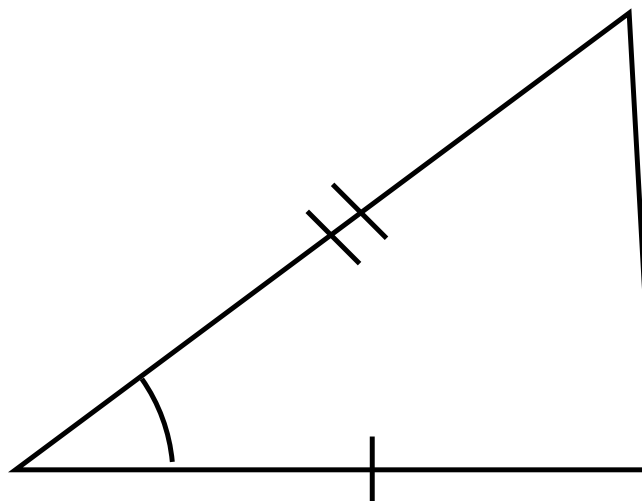
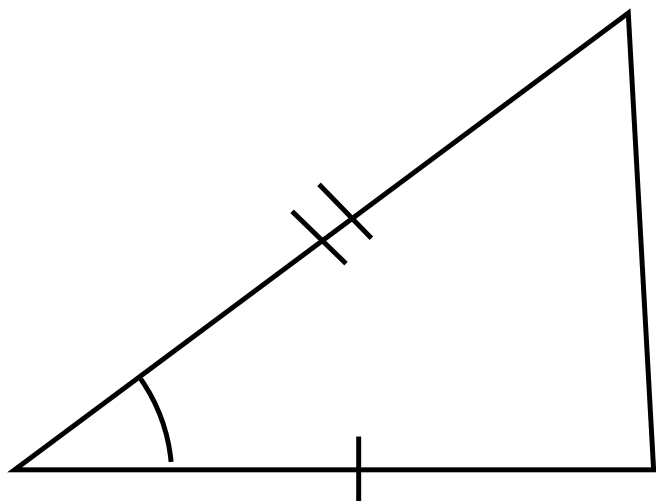
(also, $AC = LN$)

Marking Congruent Triangles

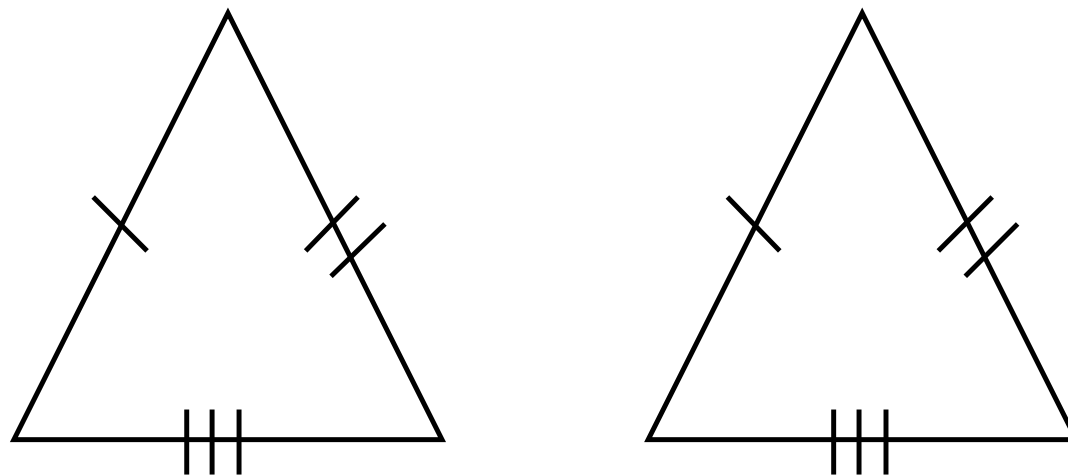
Angle-Side-Angle (ASA)



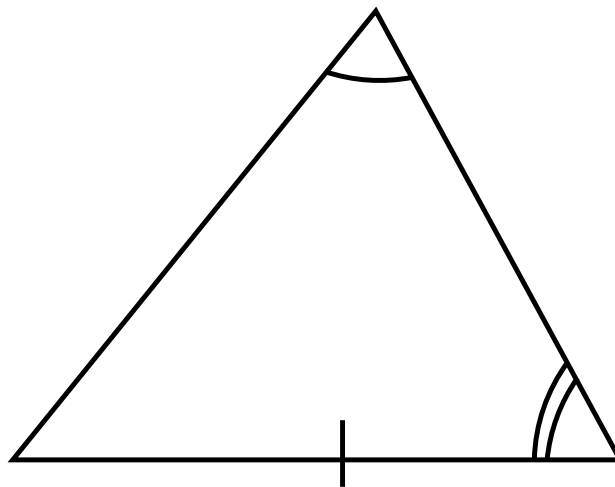
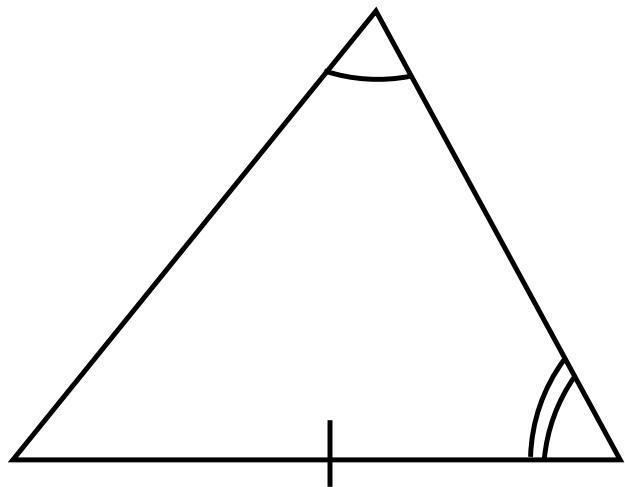
Side-Angle-Side (SAS)



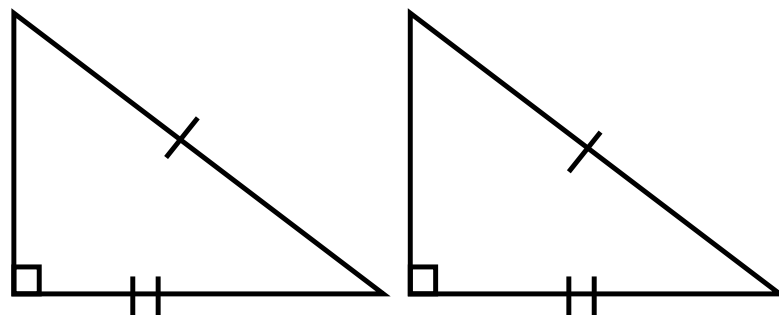
Side-Side-Side (SSS)



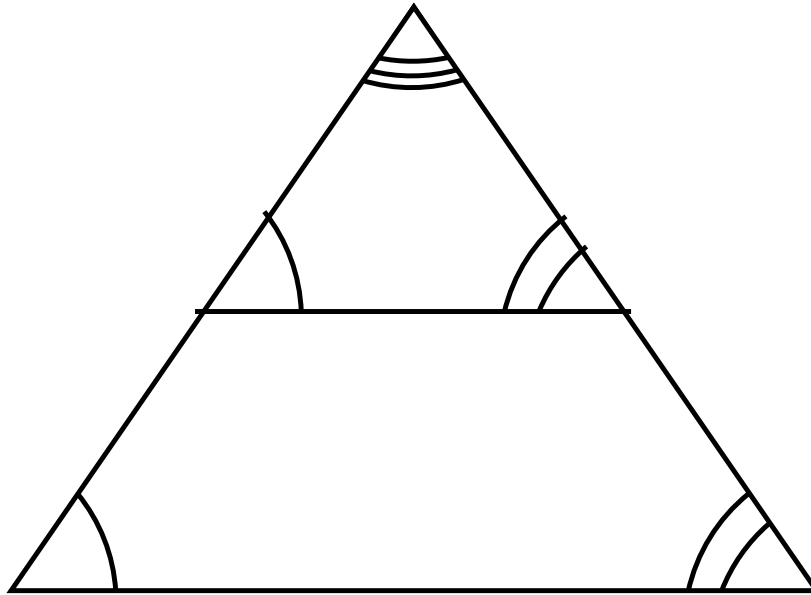
Angle-Angle-Side (AAS)



Hypotenuse-Leg (HL)

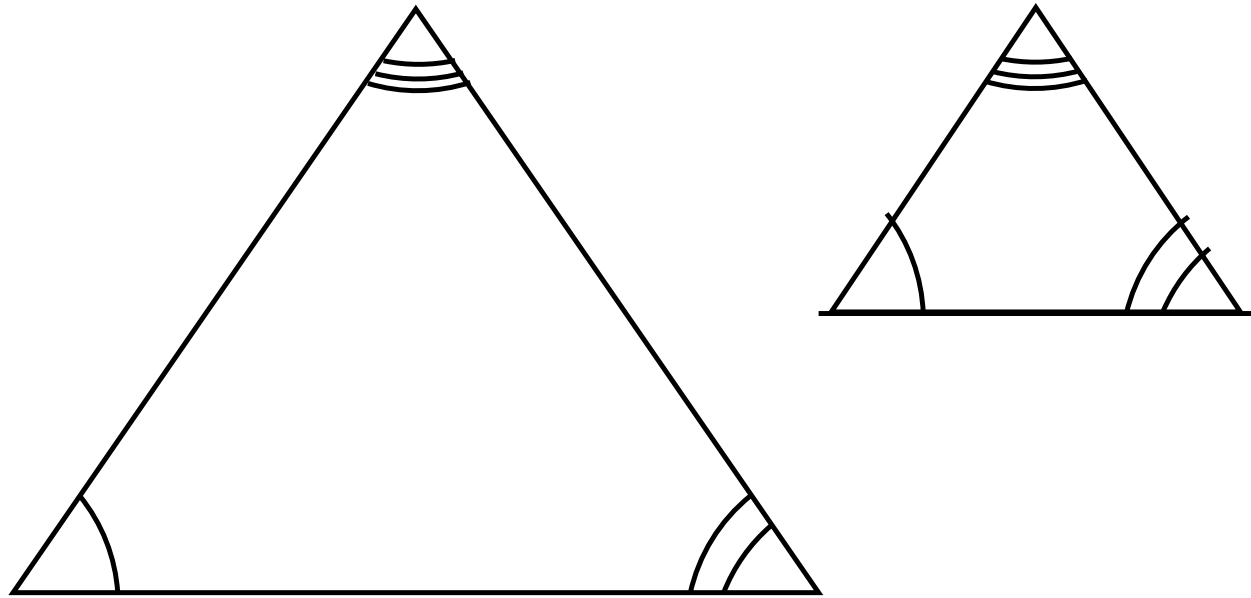


Does AAA work?

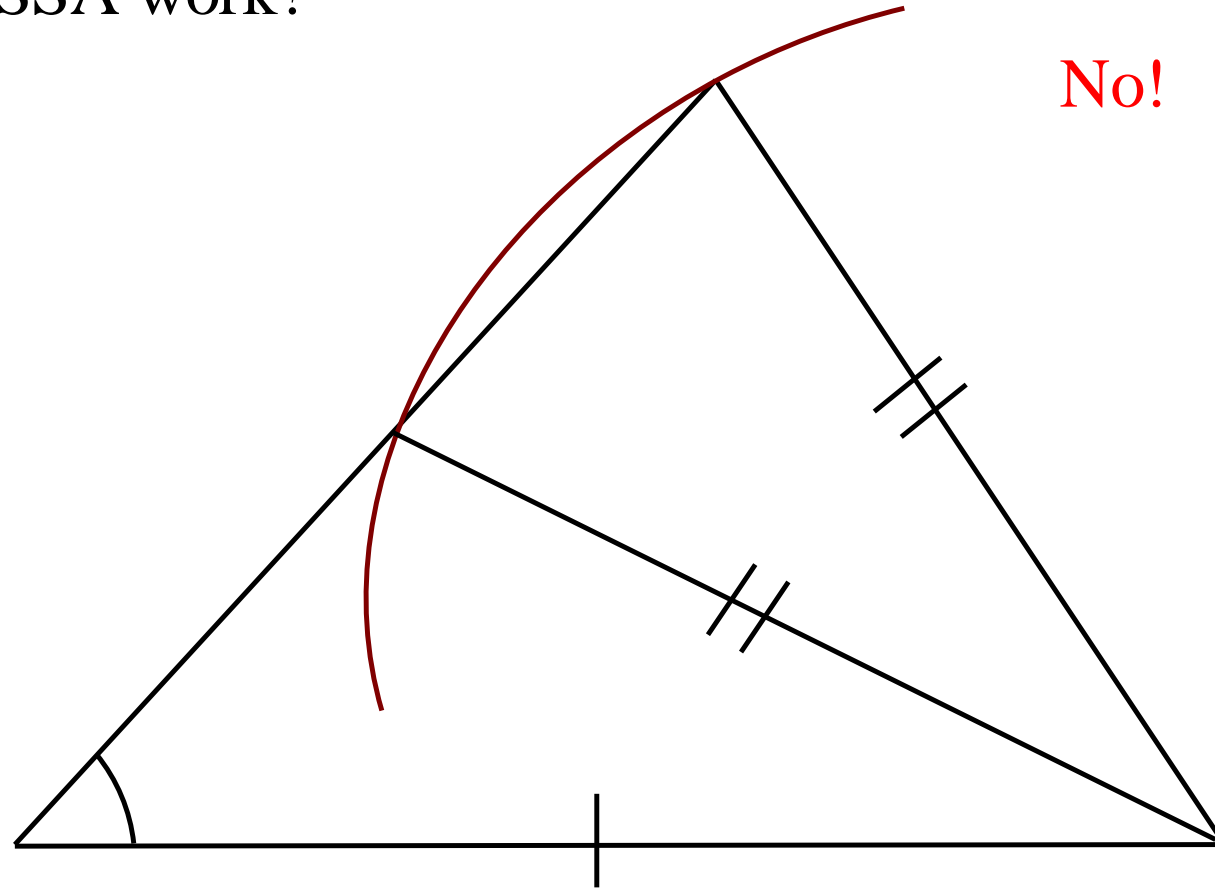


Does AAA work?

NO!



Does SSA work?



There is no SSA in geometry!

Very Important

Other than the “given” information, you can only mark three things:

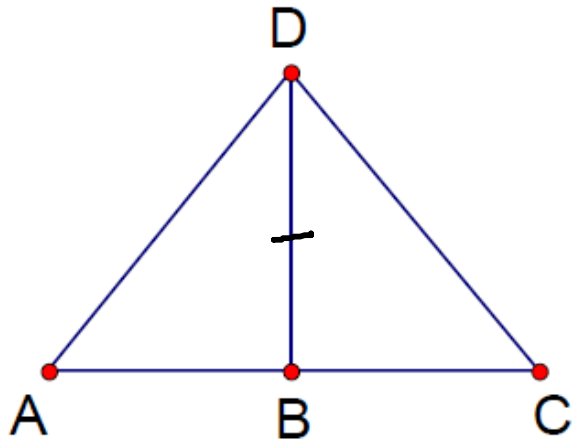
1. Shared Side (Overlapping Side)

or a Shared Angle

2. Vertical Angles

3. Alternate Interior Angles (only if lines parallel).

Shared Side



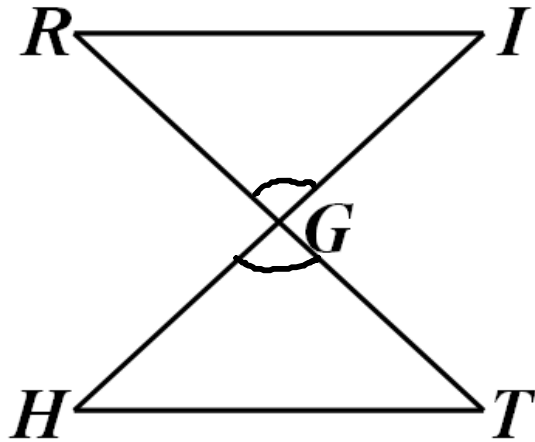
statement

$$\overline{DB} \cong \overline{DB}$$

reason

Reflex.

Vertical Angles



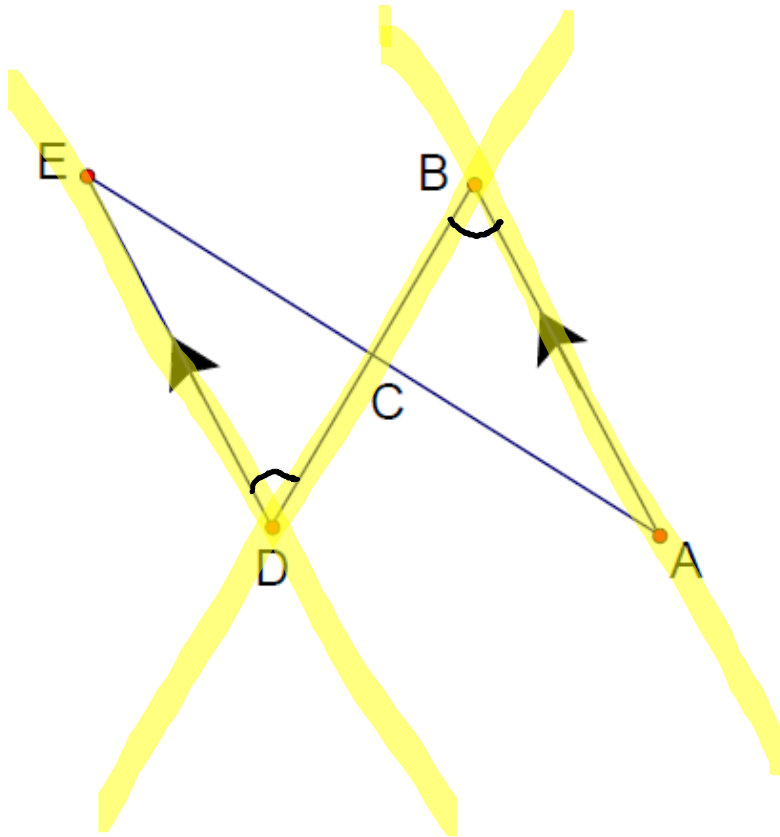
statement

$$\angle RGI \cong \angle HGT$$

reason

vert. \angle 's

Alternate Interior Angles (only if lines parallel)



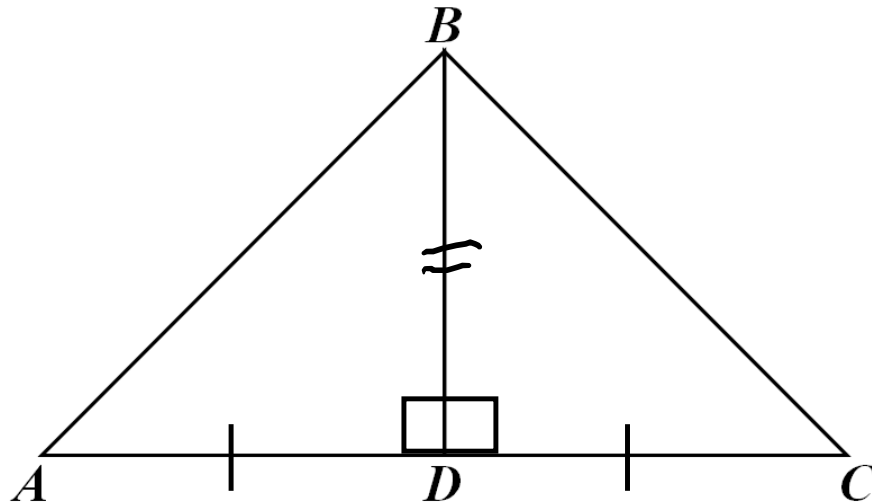
statement

$$\angle B \cong \angle D$$

reason

Alt. Int. \angle 's

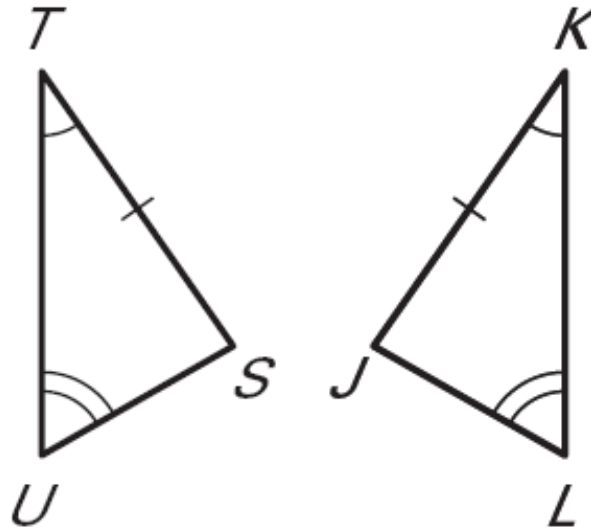
Decide whether the triangles are congruent. Explain your reasoning.



Yes, SAS

SSS
SAS
ASA
AAS
HL

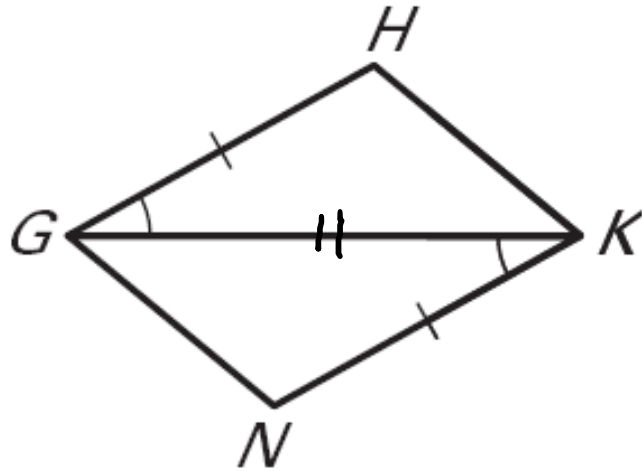
Decide whether the triangles are congruent. Explain your reasoning.



Yes, AAS

SSS
SAS
ASA }
AAS }
~~HL~~

Decide whether the triangles are congruent. Explain your reasoning.



Yes, SAS

SSS

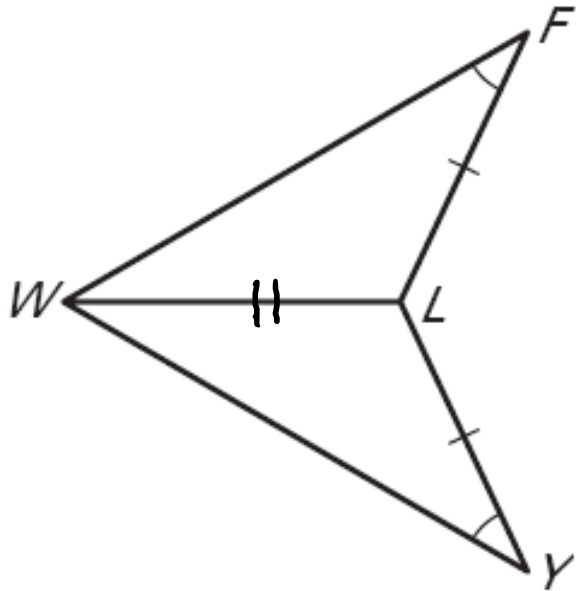
SAS

ASA

AAS

HL

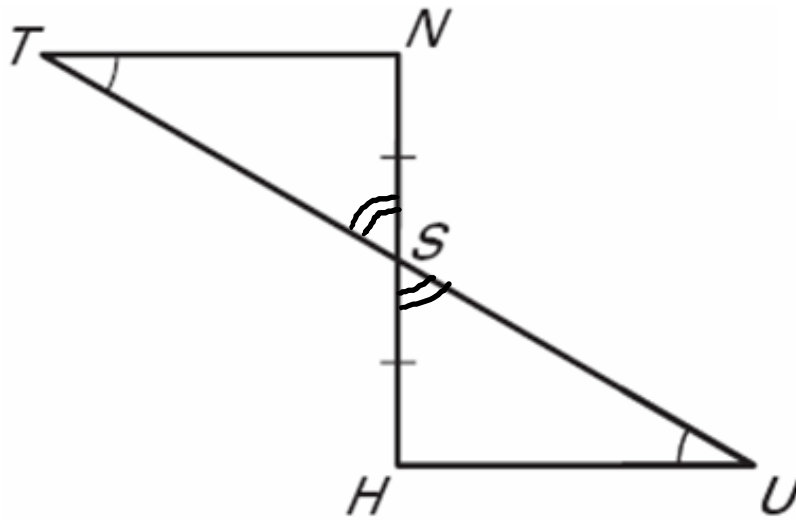
Decide whether the triangles are congruent. Explain your reasoning.



No, SSA doesn't work!

SSS
SAS }
~~ASA~~
AAS
HL

Decide whether the triangles are congruent. Explain your reasoning.



Yes,

AAS

SSS

SAS

ASA

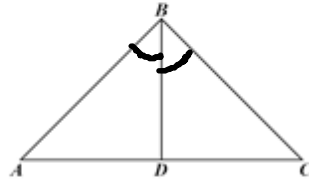
AAS

~~HL~~

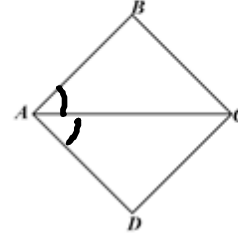
How to Mark:

- **Angle Bisectors:**

" \overline{BD} bisects $\angle ABC$ "

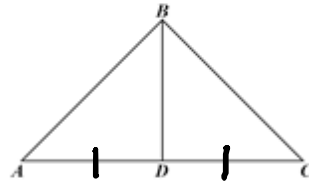


" \overline{AC} bisects $\angle BAD$ "

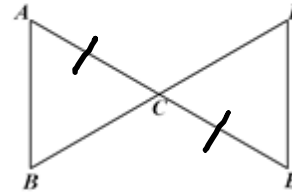


- **Segment Bisectors:**

" \overline{BD} bisects \overline{AC} "

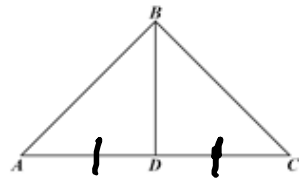


" \overline{BD} bisects \overline{AE} " or " C bisects \overline{AE} "

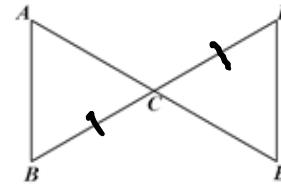


- **Midpoints:**

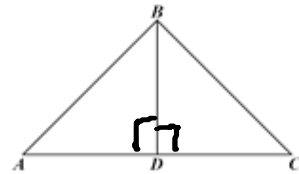
"D is midpoint of \overline{AC} "



"C is midpoint of \overline{BD} "

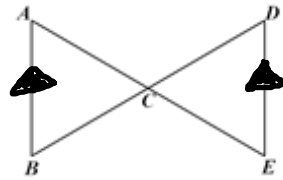


- **Perpendicular Lines:** " $\overline{BD} \perp \overline{AC}$ "



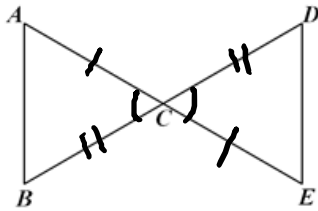
- **Parallel Lines:**

" $\overline{AB} \parallel \overline{ED}$ "



*Remember: Parallel does NOT mean Congruent,
but you can get congruent alt. int. \angle 's

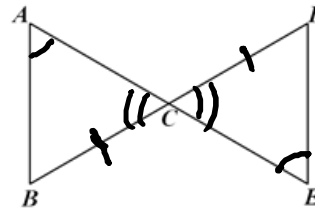
1. C bisects \overline{AE} and \overline{BD}



$$\triangle ABC \cong \triangle EDC$$

by SAS

2. $\angle A \cong \angle E$, $\overline{BC} \cong \overline{DC}$

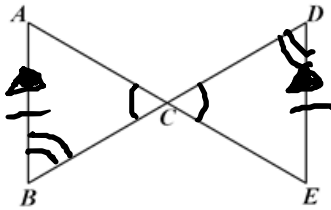


$$\triangle ABC \cong \triangle EDC$$

by AAS

SSS
SAS
ASA
AAS
HL

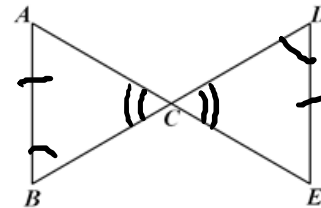
3. $\overline{AB} \parallel \overline{ED}$, $\overline{AB} \cong \overline{ED}$



$$\triangle BCA \cong \triangle DCE$$

by AAS

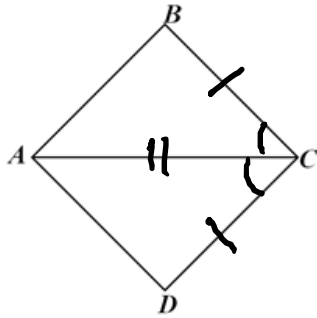
4. $\angle B \cong \angle D$, $\overline{AB} \cong \overline{ED}$



$$\triangle CAB \cong \triangle CED$$

by AAS

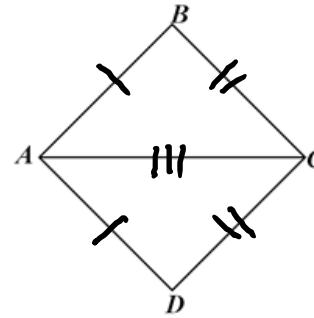
5. \overline{AC} bisects $\angle BCD$, $\overline{BC} \cong \overline{DC}$



$$\triangle ACB \cong \triangle ACD$$

by SAS

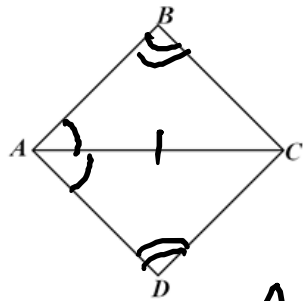
6. $\overline{AB} \cong \overline{AD}$, $\overline{BC} \cong \overline{DC}$



$$\triangle CAB \cong \triangle CAD$$

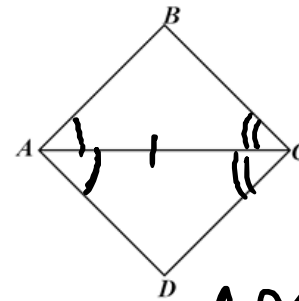
by SSS

7. $\angle BAC \cong \angle DAC$, $\angle B \cong \angle D$



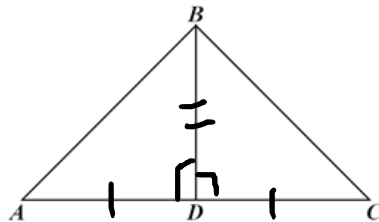
$\triangle BCA \cong \triangle DCA$
by AAS

8. \overline{AC} bisects $\angle BAD$ and $\angle BCD$



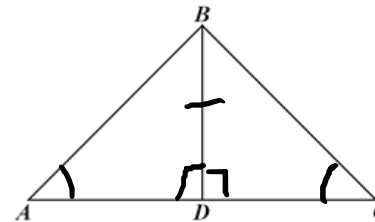
$\triangle ABC \cong \triangle ADC$
by ASA

9. $\overline{BD} \perp \overline{AC}$, D is midpoint of \overline{AC}



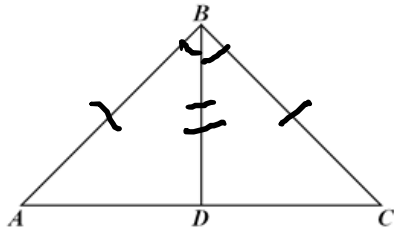
$\triangle BAD \cong \triangle BCD$
by SAS

10. $\overline{BD} \perp \overline{AC}$, $\angle A \cong \angle C$



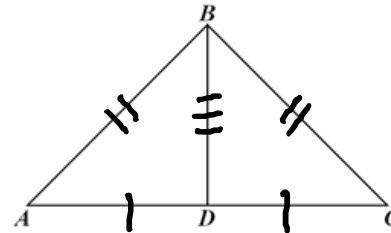
$\triangle BAD \cong \triangle BCD$
by AAS

11. \overline{BD} bisects $\angle ABC$, $\overline{BA} \cong \overline{BC}$



$\triangle ADB \cong \triangle CDB$
by SAS

12. \overline{BD} bisects \overline{AC} , $\overline{BA} \cong \overline{BC}$



$\triangle ADB \cong \triangle CDB$
by SSS