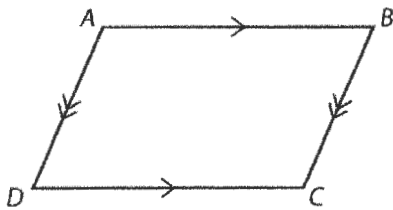


Unit 3 Review

Use the figure for 1–3. ABCD is a Parallelogram.



1. \overline{AB} is congruent to what other segment?

\overline{CD}

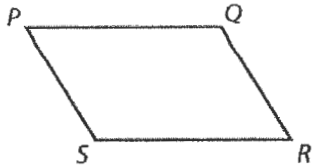
2. $\angle D$ is congruent to what other angle?

$\angle B$

3. $\angle D$ is supplementary to what other angles?

$\angle A$ & $\angle C$

Use parallelogram PQRS for 4–6.



4. If $m\angle P = 2x^\circ$, $m\angle R = (x + 31)^\circ$, find the value for x .

$$2x = x + 31$$

$$x = 31$$

5. Using your answer from problem 4, find the measure of all four angles.

$$m\angle P = 2(31) = 62 \quad m\angle Q = 180 - 62 = 118$$

$$m\angle R = 62 \quad m\angle S = 118$$

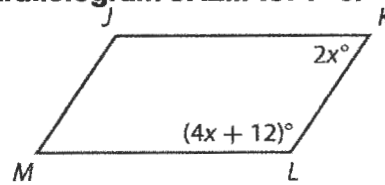
6. If $QR = 16$ and $PS = 3y - 5$, find the value for y .

$$3y - 5 = 16$$

$$3y = 21$$

$$y = 7$$

Use parallelogram JKLM for 7–8.



7. What is the value of x ?

$$4x + 12 + 2x = 180$$

$$6x + 12 = 180$$

$$6x = 168$$

$$x = 28$$

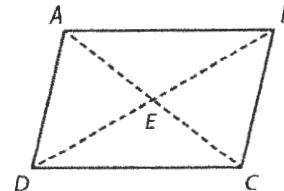
8. What are the measures of all the interior angles of the parallelogram?

$$m\angle K = 2(28) = 56 \quad m\angle L = 4(28) + 12 = 124$$

$$m\angle M = 56 \quad m\angle J = 124$$

Use the following information for 9–13.

In parallelogram CDEF, $AE = 3x + 4$, $EC = 2x + 8$, $BE = 4y + 1$, and $BD = 18$.



9. What is the value of x ?

$$3x + 4 = 2x + 8$$

$$x = 4$$

10. What is the value of y ?

$$BD = 18 \rightarrow BE = 9$$

$$4y + 1 = 9$$

$$4y = 8$$

$$y = 2$$

11. What is the length of \overline{EC} ?

$$EC = 2(4) + 8 = 16$$

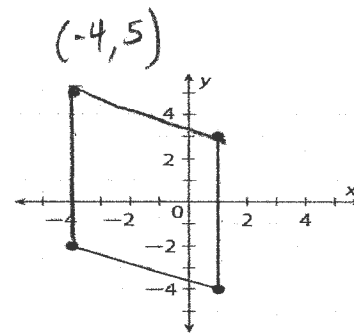
12. What is the length of \overline{AC} ?

$$AC = 2(16) = 32$$

13. What is the length of \overline{ED} ?

$$ED = BE = 9$$

14. Three vertices of a quadrilateral are shown. What is the location of the fourth vertex so that it is a parallelogram?



For Problems 15-16, use the table below. A city block is a quadrilateral bounded by four streets with given equations.

Street	Equation
Blue St.	$y = 3x - 4$
Red St.	$y = -\frac{1}{3}x + 6$
Yellow St.	$\frac{3x - y = 10}{-3x}$
Green St.	$\frac{2x + 6y = 18}{-2x}$

\rightarrow slope = 3

\rightarrow slope = $-\frac{1}{3}$

$\rightarrow \frac{-y}{-1} = \frac{-3x + 10}{-1} \rightarrow y = 3x - 10 \rightarrow$ slope = 3

$\rightarrow \frac{6}{6}y = \frac{-2x + 18}{6} \rightarrow y = -\frac{1}{3}x + 3 \rightarrow$ slope = $-\frac{1}{3}$

15. Is the block a parallelogram? Explain your reasoning,

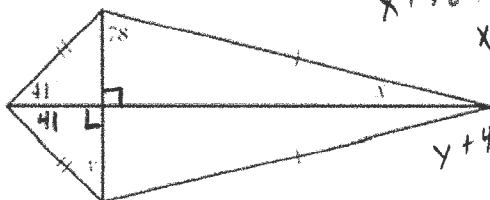
yes, two pairs of equal slopes

16. Is the block a rectangle? Explain your reasoning.

yes, 3 and $-\frac{1}{3}$ are opp. recip. so the sides are perp.

17. Solve for the variables in the kites:

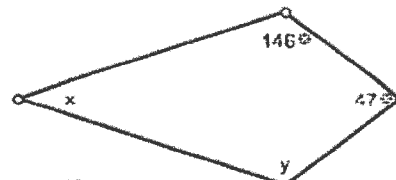
$x = 12, y = 49$



$x + 78 + 90 = 180$
 $x = 12$

$y + 41 + 90 = 180$
 $y = 49$

$x = 21, y = 146$



$x + 146 + 47 + 146 = 360$
 $x + 339 = 360$
 $x = 21$

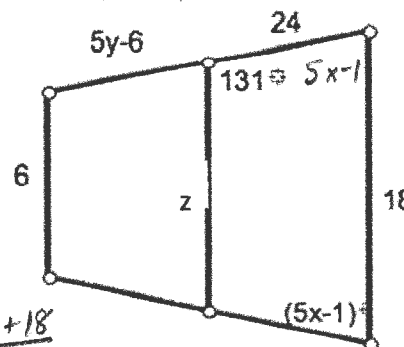
18. Solve for the variables in the isosceles trapezoid with the midsegment drawn in:

$x = 10$
 $y = 6$
 $z = 12$

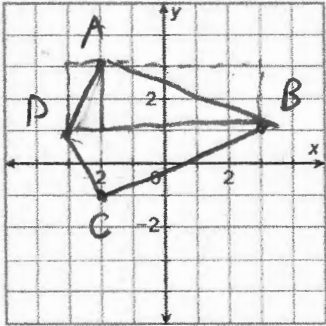
$5x - 1 + 131 = 180$
 $5x + 130 = 180$
 $5x = 50$
 $x = 10$

$5y - 6 = 24$
 $5y = 30$
 $y = 6$

$z = \frac{6 + 18}{2}$
 $= \frac{24}{2} = 12$



19. A quadrilateral has vertices $A(-2, 3)$, $B(3, 1)$, $C(-2, -1)$, and $D(-3, 1)$. Graph the points, identify the shape, and find the perimeter and area, rounding to the nearest tenth. **All work must be shown.**



Shape: kite
 Perimeter = 15.2
 Area = 12

$$\begin{aligned} \frac{AD}{2^2 + 1^2} &= x^2 \\ 4 + 1 &= x^2 \\ 5 &= x^2 \\ x &= \sqrt{5} = 2.2 \end{aligned}$$

$$\begin{aligned} \frac{AB}{5^2 + 2^2} &= x^2 \\ 25 + 4 &= x^2 \\ 29 &= x^2 \\ x &= \sqrt{29} = 5.4 \end{aligned}$$

$$P = 2.2 + 2.2 + 5.4 + 5.4 = 15.2$$

$$\frac{\triangle ADB}{\text{Area}} = \frac{1}{2}(6)(2) = 6$$

$$\text{Total Area} = 6 \cdot 2 = 12$$

20. Find each side length in the polygon below, then find the area and perimeter. Round all answers to the nearest tenth. **All work must be shown.**

Side lengths:

$$AB = \underline{6}$$

$$BC = \underline{5}$$

$$CD = \underline{3.6}$$

$$DE = \underline{8}$$

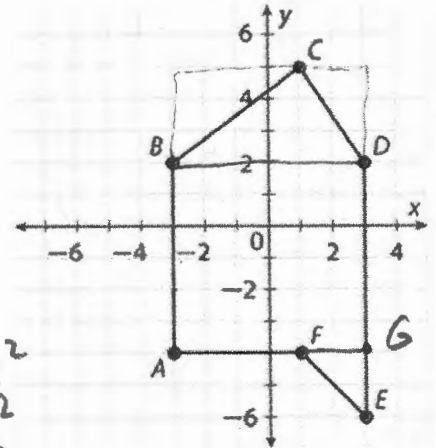
$$EF = \underline{2.8}$$

$$FA = \underline{4}$$

$$\begin{aligned} 3^2 + 4^2 &= x^2 \\ 9 + 16 &= x^2 \\ 25 &= x^2 \\ x &= \sqrt{25} = 5 \end{aligned}$$

$$\begin{aligned} 2^2 + 3^2 &= x^2 \\ 4 + 9 &= x^2 \\ 13 &= x^2 \\ x &= \sqrt{13} = 3.6 \end{aligned}$$

$$\begin{aligned} 2^2 + 2^2 &= x^2 \\ 4 + 4 &= x^2 \\ 8 &= x^2 \\ x &= \sqrt{8} = 2.8 \end{aligned}$$



$$\text{Perimeter} = \underline{29.4}$$

$$P = 6 + 5 + 3.6 + 8 + 2.8 + 4 = 29.4$$

$$\text{Area} = \underline{47}$$

$$\frac{\triangle BCD}{\text{Area}} = \frac{1}{2}(6)(3) = 9$$

$$\frac{ABDG}{\text{Area}} = 6 \cdot 6 = 36$$

$$\frac{\triangle EFG}{\text{Area}} = \frac{1}{2}(2)(2) = 2$$

$$\text{Total Area} = 9 + 36 + 2 = 47$$

$$\text{Slope: } m = \frac{y_2 - y_1}{x_2 - x_1}$$

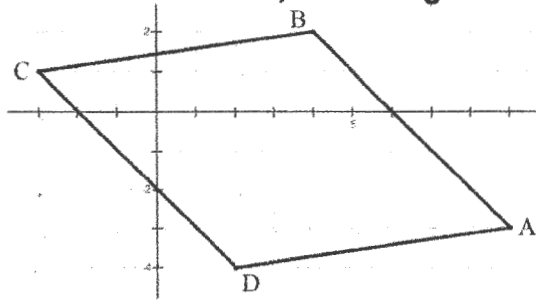
$$\text{Distance: } \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$$

$$\text{Midpoint: } \left(\frac{x_1 + x_2}{2}, \frac{y_1 + y_2}{2} \right)$$

$$\text{Area: Triangle } A = \frac{bh}{2}$$

$$\text{Rectangle } A = bh$$

For Problems 21-26, use the figure below.



21. Calculate the following slopes. Note that some segments are not drawn in the figure.

$$\text{Slope } \overline{BA} = \frac{-5}{5} = -1$$

$$\text{Slope } \overline{DA} = \frac{1}{7}$$

$$\text{Slope } \overline{CD} = \frac{-5}{5} = -1$$

$$\text{Slope } \overline{CB} = \frac{1}{7}$$

$$\text{Slope } \overline{DB} = \frac{6}{2} = 3$$

$$\text{Slope } \overline{CA} = \frac{-4}{12} = -\frac{1}{3}$$

22. Calculate the following slopes. Note that some segments are not drawn in the figure.

$$\begin{aligned} \text{Length } \overline{BA} &= \sqrt{50} \\ 5^2 + 5^2 &= x^2 \\ 25 + 25 &= x^2 \rightarrow x^2 = 50 \end{aligned}$$

$$\begin{aligned} \text{Length } \overline{DA} &= \sqrt{50} \\ 1^2 + 7^2 &= x^2 \\ 1 + 49 &= x^2 \rightarrow x^2 = 50 \end{aligned}$$

$$\begin{aligned} \text{Length } \overline{CA} &= \sqrt{160} \\ 4^2 + 12^2 &= x^2 \\ 16 + 144 &= x^2 \rightarrow x^2 = 160 \end{aligned}$$

$$\begin{aligned} \text{Length } \overline{DB} &= \sqrt{40} \\ 6^2 + 2^2 &= x^2 \\ 36 + 4 &= x^2 \rightarrow x^2 = 40 \end{aligned}$$

23. Using your calculations in Problems 21 and 22, explain how you know that the figure is a parallelogram.

two pairs of equal slopes

24. Is the figure a rectangle? Use your calculations in Problems 21 and 22 to support your answer.

no, -1 and $\frac{1}{7}$ are not perp. slopes
or diag. not same length

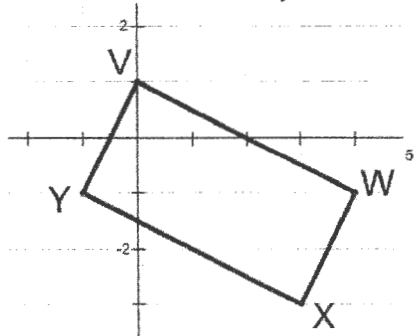
25. Is the figure a rhombus? Use your calculations in Problems 21 and 22 to support your answer.

yes, all sides have length of $\sqrt{50}$
or 3 and $\frac{1}{3}$ are perp. slopes

26. Is the figure a square? Explain how you came to that conclusion.

no, not a rectangle so can't be a square

For Problems 27-32, use the figure below.



27. Calculate the following slopes. Note that some segments are not drawn in the figure.

$$\text{Slope } \overline{VW} = \frac{-2}{4} = -\frac{1}{2}$$

$$\text{Slope } \overline{XW} = \frac{2}{1} = 2$$

$$\text{Slope } \overline{YX} = \frac{-2}{4} = -\frac{1}{2}$$

$$\text{Slope } \overline{YV} = \frac{2}{1} = 2$$

$$\text{Slope } \overline{YW} = \frac{0}{5} = 0$$

$$\text{Slope } \overline{VX} = \frac{-4}{3}$$

28. Calculate the following slopes. Note that some segments are not drawn in the figure.

$$\text{Length } \overline{VW} = \sqrt{20}$$

$$2^2 + 4^2 = x^2 \rightarrow x^2 = 20$$

$$4 + 16 = x^2 \rightarrow x^2 = 20$$

$$\text{Length } \overline{YV} = \sqrt{5}$$

$$2^2 + 1^2 = x^2 \rightarrow x^2 = 5$$

$$4 + 1 = x^2 \rightarrow x^2 = 5$$

$$\text{Length } \overline{YW} = 5$$

$$\text{Length } \overline{VX} = 5$$

$$4^2 + 3^2 = x^2 \rightarrow x^2 = 25$$

$$16 + 9 = x^2 \rightarrow x^2 = 25$$

29. Using your calculations in Problems 27 and 28, explain how you know that the figure is a parallelogram.

two pairs of equal slopes

30. Is the figure a rectangle? Use your calculations in Problems 27 and 28 to support your answer.

yes, $-\frac{1}{2}$ and 2 are perp. slopes
or diag are same length

31. Is the figure a rhombus? Use your calculations in Problems 27 and 28 to support your answer.

no, sides are diff. length
or 0 and $-\frac{4}{3}$ not perp. slopes

32. Is the figure a square? Explain how you came to that conclusion.

no, not a rhombus so
can't be a square