

# Chain Rule

These are composition functions:

$$h(x) = (3x - 2)^3$$

$$h(x) = \sqrt{3x - 2}$$

$$h(x) = \frac{1}{3x - 2}$$

$$h(x) = e^{3x-2}$$

$$\frac{d}{dx} [f(g(x))] = f'(g(x))g'(x)$$

Ex.  $f(x) = (4x^2 + 1)^7$

$$f'(x) = 7(4x^2 + 1)^6 \cdot 8x = 56x(4x^2 + 1)^6$$

Ex.  $g(x) = e^{7x}$

$$g'(x) = e^{7x} \cdot 7$$

Ex. If  $y = \sin^2 \theta$ , find  $\frac{dy}{d\theta}$ .

$$= (\sin \theta)^2$$

$$y' = 2 \sin \theta \cdot \cos \theta = \sin 2\theta$$

Ex.  $f(x) = \sec\left(\frac{x}{2}\right)$

$$f'(x) = \sec\left(\frac{x}{2}\right) \tan\left(\frac{x}{2}\right) \cdot \frac{1}{2}$$

$$\frac{x}{2} = \frac{1}{2}x$$

Pract.  $f(x) = \cos(x^2 + 1)$

$$f'(x) = -\sin(x^2 + 1) \cdot 2x$$

Pract.  $f(x) = \sqrt{3x^2 + 8x - 2}$

$$f'(x) = \frac{1}{2}(3x^2 + 8x - 2)^{-1/2}(6x + 8) = \frac{3x + 4}{\sqrt{3x^2 + 8x - 2}}$$

Pract.  $f(x) = \frac{1}{x^2 + x^4} = (x^2 + x^4)^{-1}$

$$f'(x) = -(x^2 + x^4)^{-2}(2x + 4x^3)$$

Ex.  $f(x) = x \underline{\underline{\tan(-x^2)}}$

$$f'(x) = x \cdot \underline{\underline{\sec^2(-x^2)(-2x)}} + \tan(-x^2) \cdot 1$$

$$\text{Ex. } f(x) = e^{(5x^3 - 2x)^7}$$

$$f'(x) = e^{(5x^3 - 2x)^7} \cdot 7(5x^3 - 2x)^6 (15x^2 - 2)$$

A turducken is a dish consisting of a chicken stuffed into a duck, which itself is stuffed into a turkey.

