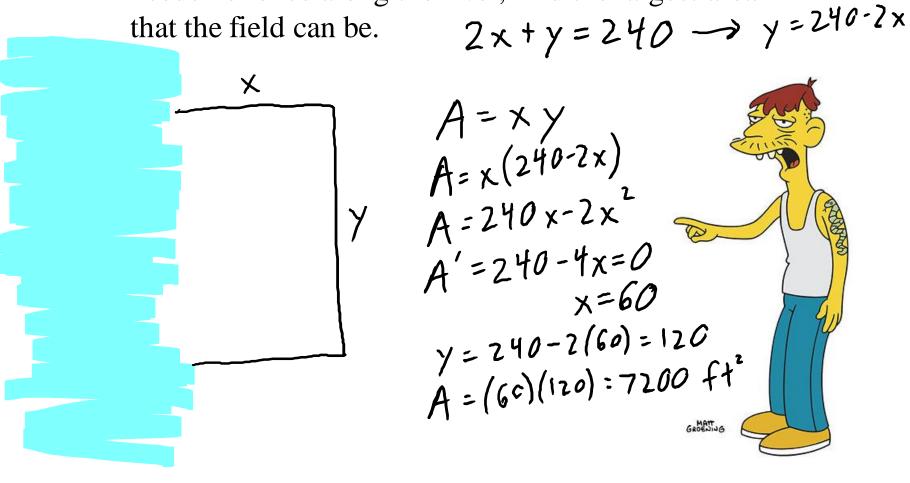
## Warm up Problems

- 1. Find and classify all critical points of  $f(x) = 4x^3 9x^2 12x + 3$
- 2. Find the absolute max./min. values of f(x) on the interval [-1,4].

## Optimization

Ex. Cletus has 240 ft. of fencing and wants to enclose a rectangular field that borders a straight river. If he needs no fence along the river, find the largest area that the field can be.  $7 \times 4 \times 240 \longrightarrow 7$ 



## Strategy for Optimization

- 1) Draw a picture, if appropriate
- 2) Write down given information, including an equation
- 3) Find the function to be optimized
- 4) Substitute to get one variable
- 5) Take the derivative
- 6) Set equal to zero and solve

Ex. The TARDIS has a square base and has a volume of 1000 m<sup>3</sup>. The Daleks have blasted all of the walls, and the Doctor wants to rebuild it as a convertible – no roof. Find the dimensions that will minimize the materials for the remaining 5 walls. (Assume it is not bigger on the inside.)

<u>Pract.</u> Sherlock has discovered a closed cylinder at a crime scene. He determines that it has a surface area of 108 cm<sup>2</sup>. What are the dimensions of such a cylinder that has the largest volume?

$$V = \pi r^{2}h$$

$$V = \pi r^{2}\left(\frac{108 - 2\pi r^{2}}{2\pi r}\right)$$

$$V = \pi r^{2}\left(\frac{108 - 2\pi r^{2}}{2\pi r}\right)$$

$$V = 54 r - \pi r^{3}$$

$$V' = 54 - 3\pi r^{2} = 0$$

$$r^{2} = \frac{18}{4\pi}$$

$$r = 2.394 cm$$

$$h = \frac{108 - 2\pi (2.394)^{2}}{2\pi (2.394)^{2}} = \frac{4.787 cm}{4.787 cm}$$



 $V = \pi r^2 h$   $S = 2\pi r h + 2\pi r^2$